

# Prediction of the complex modulus of asphalt mixture containing RAP materials from the rheological properties of mortars

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## ABSTRACT

In this paper, the properties of mortars that proportionally contain the same amount of fresh and RAP binder which can be found in the asphalt mixture, with respect to the specific material phase, are modeled with the objective of predicting the rheological behavior of the corresponding recycled mixture. For this purpose, Dynamic Shear Rheometer (DSR) tests are performed to determine the complex moduli of asphalt binders and mortars, which are then used as input in the empirical Hirsch and Witczak models. Based on the better predictions obtained from the latter, a modified formulation of the Witczak model was successfully derived to predict the mixture complex modulus directly from the experimental data of the corresponding asphalt mortar. The predictions obtained with the newly proposed expression of the Witczak model, closely match the laboratory measured complex modulus of asphalt mixtures. This can be used as input in the Mechanistic-Empirical Pavement Design Guide to analyze stress, strain, and deflection of asphalt pavements.

**Keywords:** Asphalt mixture; mortar; RAP; Hirsch model; Witczak model.

## 1. INTRODUCTION

The performance of flexible pavements is strictly associated with the modulus of asphalt mixture layers [1]. It is well known that the modulus depends on mixture volumetric properties, on the specific mix design, on loading rate and temperature [2]. Therefore, the complex modulus,  $E^*$  can be used to characterize the asphalt mixture and represents a critical input in different design methods, such as the Mechanistic-Empirical Pavement Design (MEPDG) [3] in the US or in similar procedure available in Europe [4].

The MEPDG is a pavement design and performance predicting method, developed by the National Cooperative Highway Research Program (NCHRP) in 2002 [2], that using detailed traffic loading, material properties, and environmental data, allows to compute the pavement response and to predict the incremental damage over time. The MEPDG was adopted as a pavement design guide by the American Association of State Highway and Transportation Officials (AASHTO). For this purpose, pavement engineers need a quick, easy and accurate method to obtain the complex modulus avoiding complicated and time demanding laboratory tests on mixtures. In fact, these methods require a series of expensive sampling and testing equipment, experienced laboratory personnel, and a relatively long and complex analysis. For these reasons, empirical models, such as the Hirsch [5] and Witczak [6] models were developed.

These two models are capable of predicting the complex modulus of the mixture knowing the volumetric composition and the rheological properties of the binder. However, when Reclaimed Asphalt Pavement (RAP) materials are used, the characterization of the binder present in the mixture is associated with a number of limitations. This is because the binder

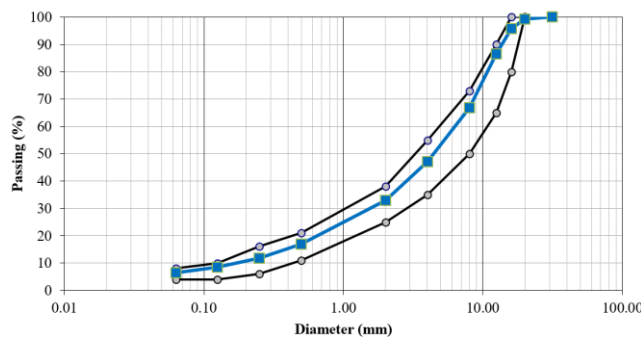
1 consists of a mix of fresh and aged RAP binder with a certain degree of blending [7]. Extraction  
2 and recovery methods are commonly used to obtain and, then, characterize the binder contained  
3 in the recycled mixture [8]. Nevertheless, several studies have demonstrated that this method is  
4 not entirely accurate since it may alter the binder properties [9,10,11], as well as, results in a  
5 complete blending of fresh and RAP binder, which may not occur in the mixture [12].

6 Recently, investigation and modeling of asphalt mortar were proposed to provide a less  
7 test-demanding and time-consuming solution for addressing the use of RAP, in comparison to  
8 the complex characterization methods required by asphalt mixture [13]. If the experimental  
9 results obtained on asphalt mortar can be used as input in predictive models to determine the  
10 rheological properties of asphalt mixture, this would provide the possibility of obtaining critical  
11 information on mixture properties also when RAP is included in the mix design, simply relying  
12 on mortar testing. Such an approach would be more practical and easier to be implemented on a  
13 routine basis, especially for laboratories in road authorities and department of transportations.

14 In this paper, the possibility of using the rheological properties of asphalt mortars,  
15 prepared with RAP, to predict the corresponding properties of mixtures containing RAP is  
16 investigated. Asphalt mortars, consisting of fresh binder and different proportion of fine RAP  
17 particles, and RAP binder, were produced in order to recreate the same amount of fresh and RAP  
18 binder in the corresponding mixture. Then, the Hirsch and Witczak models were used to predict  
19 the complex modulus of the mixture. Next, a modified expression of the Witczak model was  
20 derived so that the rheological properties ( $G^*$  and  $\delta$ ) of asphalt mortar could be used in place of  
21 the binder data for predicting the corresponding  $E^*$  for the mixture.

## 22 2. MATERIALS AND TESTS

23 In the present work, four different asphalt mixtures were produced by mixing different  
24 proportion (0%, 20%, 35% and 50%) of a German RAP source with virgin aggregates and a  
25 traditional 50/70 fresh binder. All mixes have the following common characteristics: same  
26 gradation curve (Figure 1) commonly used in Germany for binder layer; Gabbro virgin  
27 aggregates size (11/16, 8/11, 5/8, 2/5, 0/2) and RAP material obtained from a single batch; 5%  
28 total binder content by weight of the dry mix; void content target at  $4\% \pm 1.5\%$ .



29  
30 **Figure 1 Gradation Curve used for Mixtures**

31 The RAP content, 0%, 20%, 35% and 50%, was calculated in percentage by volume of  
32 the dry mixture; this corresponds to 0%, 19.6%, 34.2% and 48.5% by weight of the total mixture.  
33 All mixtures were mixed at  $160^{\circ}\text{C}$  and compacted at  $150^{\circ}\text{C}$  using a German sector compactor  
34 [14] producing slab with dimensions of 320 x 200 mm. From each slab, three cylindrical samples  
35 were cut with a diameter of 60 mm and a height of 180 mm.

36 All these mixture samples were tested in tension-compression mode (DTC-CY)  
37 according to EN 12697-26 - Annex D [15] in order to measure the complex modulus and the

1 phase angle. In order to remain in the linear visco-elastic (LVE) domain and to avoid damage in  
 2 the samples, a sinusoidal strain having a maximum amplitude of 50 microstrains was imposed to  
 3 the specimens. The tested temperatures were -20, -10, 0, 10, 20, 30, 40°C and the frequencies  
 4 were 0.1, 0.3, 1.59, 3, 5, 10 Hz. The specimen was conditioned for 5 hours at lower testing  
 5 temperatures (-20, -10, 0°C) and for 4 hours at the remaining temperatures (10, 20, 30, 40°C).

6 Asphalt binders were extracted and recovered from the mixtures using the Rotatory  
 7 Evaporator in accordance to EN 12697-3 [16]. Considering the volumetric composition of the  
 8 mixtures, the blends of fresh and RAP binder obtained from extraction are shown in Table 1.

9 **TABLE 1 Asphalt Binder Blends Composition**

Bituminous Blends	Fresh binder	RAP binder
50/70+20%RAP	80.5%	19.5%
50/70+35%RAP	65.8%	34.2%
50/70+50%RAP	51.1%	48.9%

10 In addition, SRAP mortars composed by mixing the same fresh 50/70 binder previously  
 11 used for mixtures with RAP material, passing sieve with an opening size of 0.15 mm, in different  
 12 proportions, were produced to recreate the same amount of fresh and RAP binder in the blend  
 13 and therefore, in the mixtures. Considering that the fine fraction of RAP contains 14.95% of  
 14 RAP binder with respect to the aggregate and that the fine aggregate of the RAP has a density of  
 15 2.751 g/cm<sup>3</sup>, the composition of the different mortars was obtained (Table 2). It must be noted  
 16 that a percentage of RAP of 20%, 35% and 50% in the mixture correspond to a volume  
 17 percentage of RAP particles in the mortar of 29%, 42% and 51%, respectively.

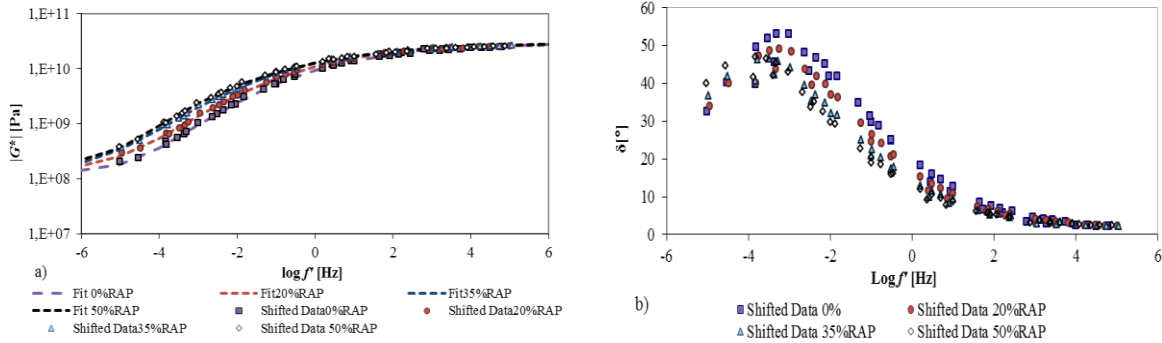
18 **TABLE 2 Composition of SRAP Mortars**

SRAP mortars	$V_p$	Fine particles of RAP	Fresh binder	RAP binder in the mortar	Total binder
SRAP 20%RAP	29	61.8%	38.2%	9.24%	47.4%
SRAP 35%RAP	42	77.7%	22.3%	11.61%	33.9%
SRAP 50%RAP	51	86.5%	13.5%	12.93%	26.5%

19 Frequency and temperature sweep tests were performed on both binders and mortars with  
 20 the Dynamic Shear Rheometer (DSR) [17]. The plate-plate geometry with three different  
 21 dimensions were used: the 4 mm plate was used for temperatures between -30°C and +10°C; the  
 22 8 mm for -10°C to +40°C; and the 25 mm for +30°C to +80°C. The tests were performed in  
 23 stress-control mode for low temperatures and in strain-control mode for high temperatures. This  
 24 mixed-mode approach was successfully used also in previous studies [18, 19].

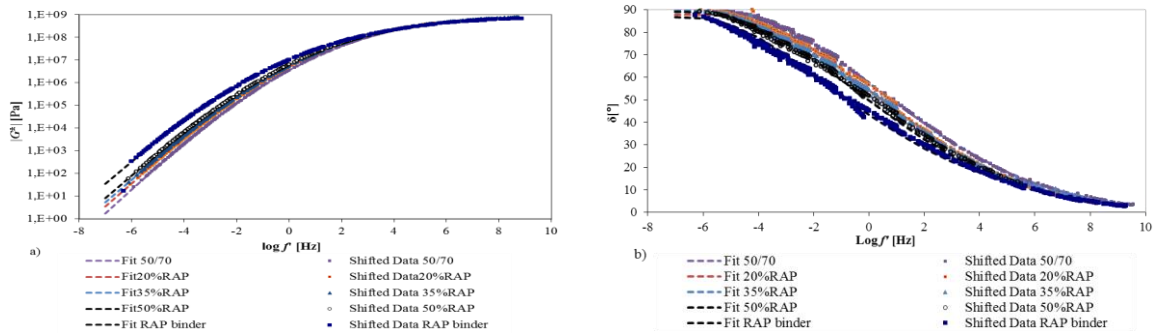
### 25 3. EXPERIMENTAL RESULTS

26 Complex modulus and phase angle were calculated from the test results and the master  
 27 curves of the different mixtures were plotted considering the Christensen Andersen Marasteanu  
 28 (CAM) model [20]. The average value of the three samples tested for each type of mixtures was  
 29 used to plot the master curves. The master curves are reported in Figures 2.

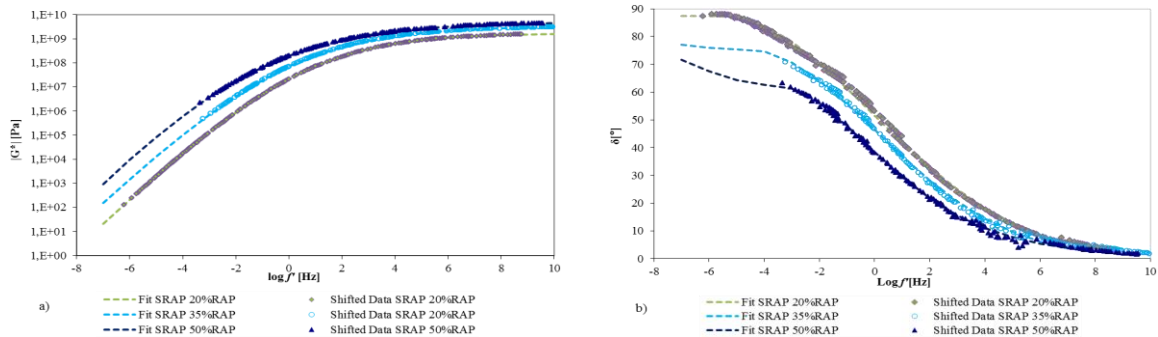


1 **Figure 2 Master Curves of the Different Mixtures: a) Complex Modulus, b) Phase Angle**

2 The complex modulus increases with the RAP content, while the phase angle decreases.  
 3 Such a trend is not entirely surprising since the mixture becomes stiffer due to the RAP binder.  
 4 The master curves of the complex modulus and of the phase angle for blends and mortars are  
 5 reported in Figure 3 and 4, respectively.  
 6



7 **Figure 3 Master Curves of a) Complex Modulus and b) Phase Angle of the blends of**  
 8 **Fresh and RAP Binder**



9 **Figure 4 Master curves of a) Complex modulus and b) phase angle of SRAP mortars**

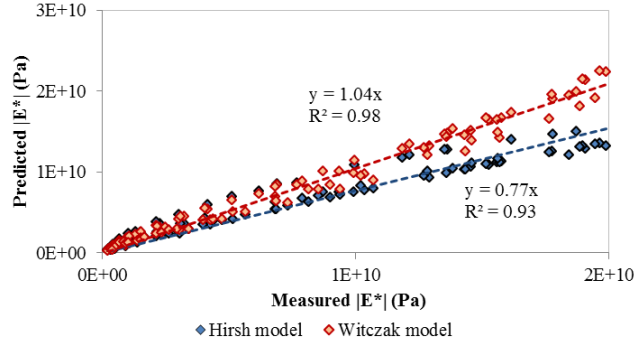
10 As shown in the previous figures, the stiffening effect due to the presence of the aged  
 11 binder and to the addition of particles is very significant. The mortar prepared with 50%RAP  
 12 presents significantly larger complex modulus and lower phase angle with respect to other  
 13 mortars; this is due to the stiffening effect of the aged binder contained in the RAP material.  
 14  
 15

16 **5. MODELING AND ANALYSES**

17 A number of empirical models were developed to predict the complex modulus of asphalt  
 18 mixture from the corresponding asphalt binder. Two of the most widely commonly used models  
 19 are those developed by Christensen et al. [21], based on the original Hirsch model [5]; and by  
 20 Bari and Witczak [6] under the NCHRP 1-40D project (Witczak 1-40D model).

## 1 5.1 Empirical models' results

2 The Hirsch model [5] and the Witczak model [6] were used to predict the modulus  $|E^*|$  of  
 3 the mixture starting from the rheological properties of the extracted binders. In Figure 5, the  
 4 Hirsch and Witczak predictions are plotted against the experimentally measured modulus for all  
 5 the mixtures. As shown, the Hirsch model underestimates the measured value by 23%, while the  
 6 Witczak overestimates the measured value by 4%.



7  
 8 **Figure 5 Predicted versus Measured Value of the Mixture Modulus  $|E^*|$  with the**  
 9 **Hirsch and Witczak Model from the Rheological Properties of Extracted Binders**

10 Figure 5 suggests that the Witczak model provides a better prediction of experimental  
 11 results in comparison to the Hirsch model for the material used in the present research. It is  
 12 important to note that both empirical models were originally derived relying on a database of a  
 13 specific set of mixtures [6, 21], therefore, their performance varies with the type of mixtures and  
 14 volumetric properties.

15 On the other hand, the Hirsch model cannot closely predict the measured  $|E^*|$  since the  
 16 formulation proposed by Christensen et al. [21] provides only a very simple assembly of the  
 17 materials' phases, which cannot capture the number of interactions occurring in a complex  
 18 mixture system. This is exemplified by the contact volume parameter,  $P_c$ , which empirically  
 19 combines the contribution of the volumetric properties into a single value, disregarding, for  
 20 example, shape and distribution of a critical material phase, such as air voids. This is also  
 21 confirmed by the attempt of other authors [22] to propose alternative expression of  $P_c$ , which is,  
 22 however, tailored to the specific material investigated.

## 23 5.3 Calibration of the Witczak model

24 Since the Witczak model shows better predictions compared to the Hirsch model for the  
 25 mixture investigated in this study, the parameters of the Witczak model, reported in Equation 1,  
 26 were fitted to directly link mortar and mixture properties.

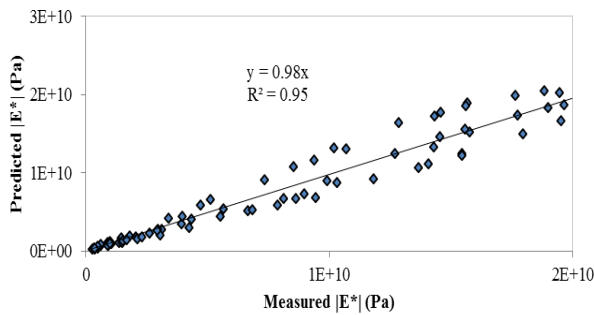
$$\begin{aligned}
 \log E^* = & -a + b |G_{mortar}^*| (6.65 - 0.032\rho_{200} + 0.0027(\rho_{200})^2 + 0.011\rho_4 - 0.0001(\rho_4)^2 + \\
 & + 0.006\rho_{38} - 0.00014(\rho_{38})^2 - 0.08V_a - 1.06 \left( \frac{V_{beff}}{V_{beff} + V_a} \right) + \\
 & + \frac{2.56 + 0.03V_a + 0.71 \left( \frac{V_{beff}}{V_{beff} + V_a} \right) + 0.012\rho_{38} - 0.0001(\rho_{38})^2 - 0.01\rho_{34}}{1 + e^{(-c-d \log(G_{mortar}^*) + e \log(\delta_{mortar}))}}
 \end{aligned} \tag{1}$$

28 where  $|E^*|$  is the complex modulus of mixture (psi),  $|G_{mortar}^*|$  is the complex shear modulus  
 29 of mortar (psi),  $\rho_{200}$  is the percentage passing #200 sieve,  $\rho_4$  is the cumulative percentage  
 30 retained on #4 sieve,  $\rho_{38}$  is the cumulative percentage retained on 3/8 in sieve,  $\rho_{34}$  is the

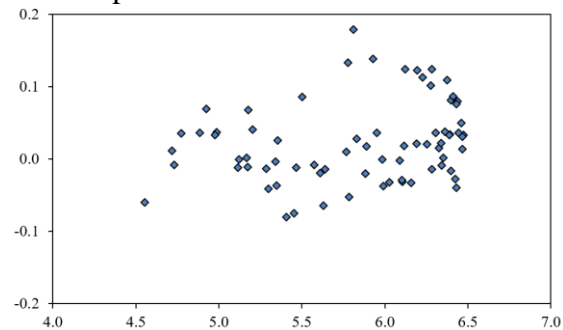
1 cumulative percentage retained on 3/4 in sieve,  $V_a$  are the air voids (% by volume),  $V_{beff}$  is the  
2 effective binder content,  $\delta_{mortar}$  is the mortar phase angle.

3 Based on nonlinear optimization, the initial parameters of the Witczak model, associated  
4 with the complex modulus and phase angle of the mortar ( $a$ ,  $b$ ,  $c$ ,  $d$ ,  $e$ ) were estimated. For this  
5 purpose, all the mixtures composed with different percentage of RAP were analyzed. The  
6 parameters obtained from the optimization process are:  $a=4.215$ ,  $b=1.493$ ,  $c=10.111$ ,  $d=0.327$   
7 and  $e=5.876$ .

8 Figure 6 presents a comparison between the Witczak model predicted complex modulus  
9 (using the rheological data of the mortar) and the measured experimental data. A strong linear  
10 trend can be observed as demonstrated by the very high regression coefficient  $R^2=0.95$ . Given a  
11 slope of 0.98, the model underpredicts the measured value by only 2%. In Figure 7, the residual  
12 plot (residuals versus predicted values) is presented. Residuals are considered to have a  
13 horizontal band pattern. Therefore, the calibrated model seems to reasonably predict  $|E^*|$  of the  
14 asphalt mixtures investigated, starting from tests results on asphalt mortars.



**Figure 6 Witczak Predicted versus Measured Complex Modulus of the Mixture from Rheological Properties of Mortars**



**Figure 7 Residual Plots of the Calibrated Witczak Model**

## 15 6. CONCLUSIONS

16 In this work, the empirical Hirsch and Witczak models were used to determine the  
17 complex modulus of asphalt mixture, starting from the rheological properties of the  
18 corresponding binder extracted and recovered from mixtures composed with different percentage  
19 of RAP materials (0, 20, 35, 50%). The Hirsch model was found to underpredict the measured  
20 value, while the Witczak model leads to slightly higher values of the complex modulus. In  
21 addition, it was found that the Witczak model better predicts the experimental values. Based on  
22 this initial analysis, the Witczak model parameters associated with the behavior of bituminous  
23 component were successfully calibrated to determine the complex modulus of the mixture  
24 knowing its volumetric properties and the rheological response of the corresponding mortar.

25 The new formulation showed a very close matching between experimental and Witczak's  
26 predicted complex modulus. In addition, the mixture behavior is directly obtained from tests on  
27 asphalt mortar, without relying on the extraction and recovery of RAP binder. Such an approach  
28 reduces the amount of time-consuming and costly tests of asphalt mixtures and will allow testing  
29 the RAP binder as is after the milling process avoiding any treatments and manipulations which  
30 may alter the recycled material properties. The predicted values of the mixture complex modulus  
31 can be used as input in the MEPDG [3] in order to evaluate the response asphalt pavement in  
32 terms of stress, strain, and deflection.

## 1 REFERENCES

- 2 [1] Loulizi, A., Flintsch, G., Al-Qadi, I., Mokarem, D. Comparing Resilient Modulus  
3 and Dynamic Modulus of Hot-Mix Asphalt as Material Properties for Flexible Pavement Design.  
4 Transport Research Record. Vol. 1970 pp. 161-170. 2006.
- 5 [2] Witczak, M. W., Kaloush, K., Pellinen, T., and ElBasyouny, M. Simple Performance  
6 Test for Superpave Mix Design. NCHRP Report 465, Washington, DC. 2002.
- 7 [3] AASHTO MEPDG-2. Mechanistic-Empirical Pavement Design Guide: A Manual of  
8 Practice. American Association of State Highway and Transportation Officials. 2015.
- 9 [4] Wistuba, M., and Walther, A. Consideration of Climate Change in the Mechanistic  
10 Pavement Design, Road Material and Pavement Designs, Vol. 14 Supplement 1, pp. 227-241.  
11 2013. doi: 10.1080/14680629.2013.774759
- 12 [5] Hirsch, T., J. Modulus of elasticity of concrete affected by elastic moduli of cement  
13 paste matrix and aggregate. Journal of the American Concrete Institute, 59(3), pp. 427-452. 1962.
- 14 [6] Bari, J., and Witczak, M. Development of a new revised version of the Witczak E  
15 Predictive Model for hot mix asphalt mixtures. Journal of the Association of Asphalt Paving  
16 Technologist, Vol. 75, pp. 381-423. 2006,
- 17 [7] Rad, F. Y., Sefidmazgi, N. R. and Bahia, H., Application of Diffusion Mechanism to  
18 Study Degree of Blending Between Fresh and RAP Binder in Dynamic Shear Rheometer,  
19 Transportation Research Record, Vol. 2444, pp. 71-77. 2014.
- 20 [8] Jiménez del Barco Carrión, A., Lo Presti, D., and Airey, G., D. Binder design of  
21 high RAP content hot and warm asphalt mixture wearing courses. Road Materials and Pavement  
22 Design. Vol. 16(1), pp. 460-474. 2015.
- 23 [9] Stroup-Gardiner, M., and Nelson, J. Use of Normal Propyl Bromide Solvents for  
24 Extraction and Recovery of Asphalt Cements. Report 00-06, National Asphalt Pavement  
25 Association (NAPA). 2014.
- 26 [10] Ma, T., and Zhang, D. Y. Research on Influence and Modification of Extraction and  
27 Recovery Experiments for SBS Modified Asphalt, Journal of Southeast University, Vol. 40(5),  
28 pp. 511–523. 2008.
- 29 [11] Ma, T., and Huang, X. Recycling Law of Aged Asphalt based on Composite Theory  
30 of Material, Journal of Southeast University, Vol. 38(3), pp. 520–524. 2008.
- 31 [12] Kriz, P., Grand, D., L., Veloza, B., A., Gale, M., J., Blahey, A., G., Brownie, J., H.,  
32 Shirts, R., D., and Maccarone, S. Blending and Diffusion of reclaimed asphalt pavement and  
33 virgin binders. Road Materials and Pavement Design, Vol. 15(1). pp. 78-112. 2014.
- 34 [13] Ma, T., Mahmoud, E., and Bahia, H., U. Development of testing procedure for the  
35 estimation of RAP binder Low Temperature properties without extraction. Transport Research  
36 Record. Vol. 2179. 2009. doi: 10.3141/2179-07
- 37 [14] Wistuba, M. The German Segmented Steel Roller Compaction Method – State-of-  
38 the-Art Report, International Journal of Pavement Engineering, Vol. 17(1), pp. 81-86. 2014. doi:  
39 10.1080/10298436.2014.925555
- 40 [15] EN 12697-26. Bituminous mixtures. Test methods for hot mix asphalt. Stiffness,  
41 European Committee for Standardization. 2012.
- 42 [16] EN 12697-3. Bituminous mixtures. Test methods for hot mix asphalt. Bitumen  
43 recovery: Rotary evaporator, European Committee for Standardization. 2013.
- 44 [17] EN 14770. Bitumen and bituminous binders. Determination of complex shear  
45 modulus and phase angle - Dynamic Shear Rheometer (DSR). European Committee for  
46 Standardization. 2012.

1 [18] Riccardi, C., Cannone Falchetto, A., Losa, M., and Wistuba, M. P. Development of  
2 Simple Relationship between Asphalt Binder and Mastic based on Rheological Tests, Road  
3 Materials and Pavement Design. 2016. doi: 10.1080/14680629.2016.1230514  
4 [19] Riccardi, C., Cannone Falchetto, A., Wang, D., and Wistuba, M. P., 2017. Effect of  
5 Cooling Medium on Low Temperature Properties of Asphalt Binder, Journal of the Associations  
6 of Asphalt Paving Technologists (in press).  
7 [20] Marasteanu, M. O., and Anderson, D. A. Improved Model for Bitumen Rheological  
8 Characterization. Presented at Eurobitume Workshop on Performance Related Properties for  
9 Bituminous Binders, Luxembourg, Belgium, May 1999.  
10 [21] Christensen, D., Pellinen, T. and Bonaquist, R. F. Hirsch Model for Estimating the  
11 Modulus of Asphalt Concrete, Journal of the Association of Asphalt Paving Technologists, Vol.  
12 72, pp. 97-121. 2003.  
13 [22] Zofka, A. Investigation of asphalt concrete creep behavior using 3-point bending test.  
14 Dissertation. University of Minnesota. 2007.