

Exploring Master Curve Parameters to Distinguish between Mixture Variables

Mirkat Oshone¹, Jo Sias Daniel², Eshan Dave³, Amy Epps Martin⁴, Fawaz Kaseer⁵, Reyhaneh Rahbar-Rastegar⁶

(¹ University of New Hampshire, 33 Academic Way, NH, USA, mto1@wildcats.unh.edu)

(² University of New Hampshire, 33 Academic Way, NH, USA, jo.daniel@unh.edu)

(³ University of New Hampshire, 33 Academic Way, NH, USA, eshan.dave@unh.edu)

(⁴ Texas A&M University, College Station, TX, USA, a-eppsmartin@tamu.edu)

(⁵ Texas A&M University, College Station, TX, 77843, USA, fawazkaseer@tamu.edu)

(⁶Purdue University, West Lafayette, IN, USA, rrahbar@purdue.edu)

ABSTRACT

It is well known that mixture variables such as aging level, rejuvenator dosage, recycled binder ratio, and binder grade alter the rheological properties of asphalt concrete mixtures, subsequently affecting their performance in the field. Rheological evaluation can be employed through linear viscoelastic characterization in the form of dynamic modulus and phase angle master-curves. This study investigated the ability of dynamic modulus and phase angle master-curve parameters to capture the changes in mixture properties caused by aging, addition of rejuvenator, use of recycled material and change in binder grade by performing a comprehensive statistical analysis on 29 mixtures. Evaluated parameters included: the mixture Glover-Rowe parameter, inflection point frequency ($-\beta/\gamma$), difference between the glassy modulus and the inflection point modulus (γ), $-\beta/\gamma$ vs γ , and the lower and upper asymptotes of the sigmoidal master-curve. The effect of changes in mixture variables on master-curve parameters are qualitatively compared to expected mixture field performance as well. The study indicated the ability of all master-curve parameters to capture the effect of aging. In addition, the change in recycled material binder content is captured well by the G-R parameter, while $-\beta/\gamma$ and δ values were impacted by binder low temperature grade.

Keywords: dynamic modulus and phase angle master curve, master curve shape parameters, mixture variables, mixture performance

1. INTRODUCTION

It is well known that the common mixture variables such as aging level, rejuvenator use and dosage, content and type of recycled materials (Reclaimed Asphalt Pavement (RAP) or Recycled Asphalt Shingles (RAS)), and binder grade alter the rheological properties of asphalt concrete mixture which are important for design and modeling of asphalt pavements. The ability to understand the changes in rheological properties caused by changes in the mixture variables is beneficial to quantify the effect on mixture field performance. Rheological evaluation of asphalt concrete mixtures is commonly done by measuring the dynamic modulus ($|E^*|$) and phase angle (ϕ) to produce $|E^*|$ and ϕ master-curves for a range of temperature and frequency combinations. These two parameters can be determined at the mixture design or production stage directly by performing the complex modulus test (1) or indirectly from relaxation modulus and creep compliance tests through interconversion (2, 3). Moreover, different researchers have developed

1 regression equations that can be used to determine dynamic modulus (4, 5, and 6) as well as
 2 phase angle (7, 8) values mainly from mixture design parameters. A study by Oshone et al. (9)
 3 proposed an approach for obtaining dynamic modulus master-curves from falling weight
 4 deflectometer (FWD) measurements taken throughout the pavement life. Due to the increasingly
 5 reliable and versatile ways to determine $|E^*|$ and ϕ master curves at different stages of the
 6 pavement life, researchers have tried to investigate the ability of master-curve parameters to
 7 track the changes in mixture properties due to different mixture variables (10, 11, 12). However,
 8 previous studies have not focused on a comprehensive statistical analysis to link the changes in
 9 mixture variables to master curves parameters.

10 In this study, a comprehensive statistical analysis was performed to investigate the ability
 11 of master-curve parameters to capture changes in mixture properties due to aging level, the
 12 addition of RAP/RAS, dosage of rejuvenator, and change in binder grade. Evaluated master-
 13 curve parameters are the mixture Glover-Rowe (G-R) parameter which relates $|E^*|$ and ϕ in
 14 Black space, and master-curve shape parameters (log of the inflection point frequency ($-\beta/\gamma$), log
 15 of the distance between the glassy modulus and the inflection point modulus (γ), $-\beta/\gamma$ vs γ and
 16 lower and upper asymptotes of the sigmoidal form of the master curve). The effect of the
 17 changes in the parameters on performance due to variation in the mixture variables is described
 18 qualitatively. It is believed that the master curve parameters identified in this study can be used
 19 by mixture specifiers and producers during design, construction and service life of the pavement
 20 to determine the effect of the different mixture variables on performance.

21 2. MATERIALS AND METHODS

22 For this study 29 mixtures were used. The mixtures include eight mixtures from Texas,
 23 five mixtures from Nevada, three mixtures from Indiana and four mixtures from Wisconsin that
 24 are being evaluated as part of the NCHRP 9-58 project. The variables in these mixtures include
 25 aging levels (short-term oven aging (STOA) and long-term oven aging (LTOA)), rejuvenator
 26 dosage, recycled binder ratio (RBR, which defines the amount of RAP and RAS binder in the
 27 mixture as percent of total binder), binder grade (PGHT, high temperature performance grade
 28 and PGLT, low temperature performance grade) and PG spread (the difference between high and
 29 low temperature performance grade). Nine mixtures from New Hampshire (NH) are also
 30 included. These mixtures represent different percentages of RAP and RAS, binder grade and
 31 different aging levels (STOA and LTOA). The LTOA includes 5 days at 85°C on compacted
 32 specimens, and 5 days at 95°C, 24 hours at 135°C and 12 days at 95°C on loose mixture. Table 1
 33 shows the mixture variables considered for the study along with the levels considered. All the
 34 mixtures were designed to optimum asphalt content using Superpave approach and test
 35 specimens were produced at a consistent air void level.

36 $|E^*|$ and ϕ master curves were produced using isotherms measured at three temperatures
 37 and six frequencies. A generalized sigmoidal equation with five parameters (indicated in
 38 Equation 1) was used to fit the $|E^*|$ master curves: w is loading frequency, δ is the lower
 39 asymptote, α is the difference between the values of upper and lower asymptote and λ , β and γ
 40 define the shape between the asymptotes and the location of the inflection point.

$$41 \quad \log|E^*| = \delta + \frac{\alpha}{(1 + \lambda e^{[\beta + \gamma(\log w)]})^{1/\lambda}} \quad \text{Eq. (1)}$$

42 The mixture G-R parameter in Black space and master-curve shape parameters
 43 investigated in this study are described below and are illustrated in Figures 1(a) and (b).

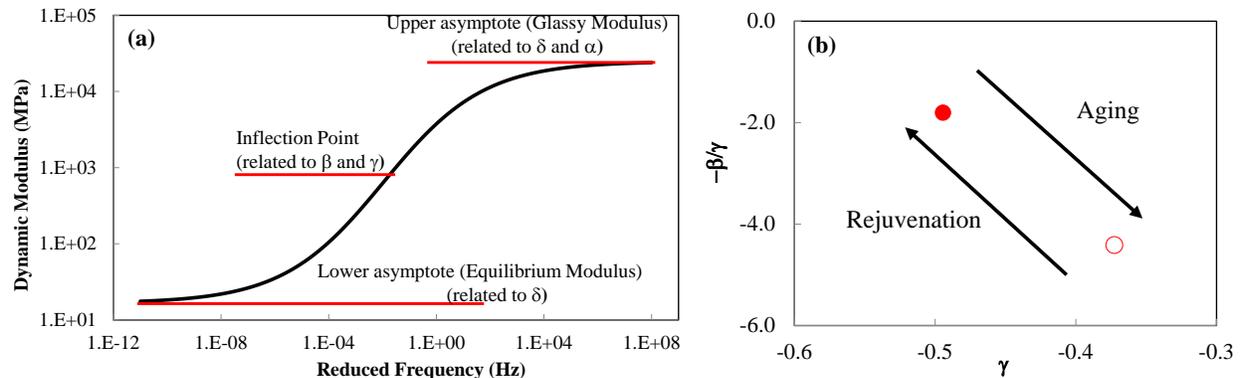
- 1 • Mixture G-R parameter ($|E^*| \cos\phi^2/\sin\phi$) combines the $|E^*|$ and ϕ values to describe the
 2 stiffness and relaxation properties of an asphalt concrete mixture. For this study the
 3 parameter was determined at 15°C and 5 rad/s to track the changes in mixture properties due
 4 to changes in mixture variables.

5 **TABLE 1 Mixtures Information**

Mixture Variables	Range of Mixture Variables				
	Texas	Nevada	Indiana	Wisconsin	New Hampshire
RBR (%)	0-50	0-30	0-42	27-36	20-30
Rejuvenator, %	0-12.5	0-2	0-3	1.2	-
PGHT, °C	64, 70	64	59	52, 58	52, 58
PGLT, °C	-22, -28	-28	-28	-28, -34	-28, -34
PG spread, °C	86, 92	92	86	86	86
Aging level	5 days 85°C ^a	5 days 85°C ^a	5 days 85°C ^a	5 days 85°C ^a	5 days at 85 °C ^a 5 days at 95 °C ^b 24 hours at 135 °C ^b 12 days at 95°C ^b

6 ^a aging on compacted specimens ^baging on loose mixture

- 7 • Log of the inflection point frequency ($-\beta/\gamma$) describes the elastic-viscous transition exhibited
 8 as a result of a shift from aggregate structure to binder dominating behavior. It marks the
 9 peak of the ϕ master curve or the inflection point in the $|E^*|$ master curve.
 10 • Log of the distance between the glassy modulus and the inflection point modulus (γ)
 11 describes the width of the relaxation spectra and is computed from the difference between the
 12 glassy modulus and inflection point modulus. As the $|E^*|$ master curve flattens, which
 13 typically happens with aging, the γ value increases.
 14 • Lower (δ) and upper ($\delta+\alpha$) asymptotes represent the maximum and minimum points of the
 15 $|E^*|$ master-curves and are primarily related to aggregate properties.
 16 • $-\beta/\gamma$ vs γ shows the log of the inflection point frequency against the log of the distance
 17 between the glassy modulus and the inflection point modulus. This is similar to the plot of
 18 crossover frequency versus rheological index for binders. The points are expected to move to
 19 bottom right with aging and to the top left corner with the addition of rejuvenators as
 20 illustrated in Figure 1(b) [13]. In this study the effects from the two parameters are combined
 21 by calculating $(-\beta/\gamma^2)$ and using the combined parameter in the regression analysis.
 22



23 **FIGURE 1 (a) $|E^*|$ Master Curve Shape Parameters (b) $-\beta/\gamma$ vs γ Plot Schematically**
 24 **showing Hypothesis for Impacts of Aging and Rejuvenation**
 25

1 A stepwise regression analysis performs an iterative screening to determine the presence
 2 of a mathematical relationship between two variables such that a linear function of one can
 3 predict the other at a given confidence level. In this study a stepwise regression analysis was
 4 utilized to identify the significance of the different mixture variables on the master-curve
 5 parameters. The analysis made inferences about the larger population to recognize the ability of
 6 master-curve parameters to capture the changes in mixture properties caused by changes in
 7 mixture variables. This was accomplished by using the p-values from the analysis as an indicator
 8 for the existence of a relationship. For this study, the common practice of utilizing p-value < 0.05
 9 is adopted and the null hypothesis is rejected for a p-value <0.05 indicating the mixture variables
 10 has contributed significantly to the changes observed in the master-curve parameter.

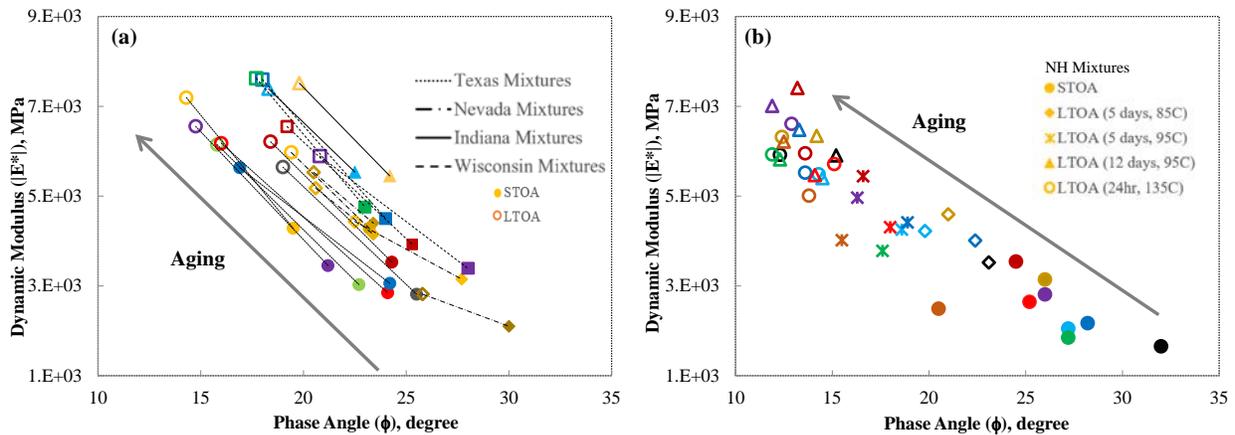
11 3. RESULTS AND DISCUSSION

12 The stepwise regression analysis performed on study mixtures was able to provide a
 13 platform to distinguish between master curve parameters that can track the changes in mixture
 14 properties due to aging level, RBR, rejuvenator dosage and binder grade. The p-values obtained
 15 from the analysis are presented in Table 2. A p-value < 0.05 was used as a threshold to identify
 16 the existence of a relationship between the mixture variables and the master-curve parameters. In
 17 other words, a p-value of <0.05 (indicated in **bold**) shows the ability of the master-curve
 18 parameter to capture the change in mixture property caused by the corresponding mixture
 19 variable.

20 **TABLE 2 p-values from Stepwise Regression Analysis**

Mixture Variables	G-R Parameter	$-\beta/\gamma$ vs γ	$-\beta/\gamma$	γ	δ	$\delta+\alpha$
Aging	<0.001	<0.001	<0.001	<0.001	<0.001	<0.001
RBR	0.05	0.57	0.20	0.55	0.91	0.18
RA	0.90	0.90	0.89	0.32	0.70	0.30
PGHT	0.16	0.37	0.29	0.05	0.35	0.20
PGLT	0.02	0.49	0.05	0.11	0.04	0.25
Δ PG	0.67	0.80	0.59	0.71	0.35	0.95

21 **Mixture G-R parameter** - The regression analysis indicated the ability of the mixture G-
 22 R parameter to capture the changes in mixture properties caused by aging, RBR and PGLT of the
 23 binder (p-value for aging <0.001, RBR=0.05 and PGLT=0.02). The changes due to aging are
 24 shown in Black space diagram (Figures 2(a) and (b)), which similarly combines the effects of
 25 $|E^*|$ and ϕ in one plot. The plot shows that with aging the points shift towards the top left
 26 implying a change to a stiffer and less viscous material. For NH mixtures the shift increases as
 27 the aging level changes from 5 days at 85°C to 5 days at 95°C followed by 12 days at 95°C and
 28 24hr at 135°C, Figure 2 (b). This increment in increasing stiffness and decreasing relaxation
 29 capacity is expected to increase the propensity of the mixture to cracking. In addition to the
 30 aging effect, the mixture G-R parameter appears to capture the effects of RBR and low
 31 temperature grade which also play a significant role in the cracking property of asphalt mixtures.
 32 The cumulative effect of these three parameters can be tracked and entered into a pavement
 33 performance prediction model to quantify the effect on field performance.
 34



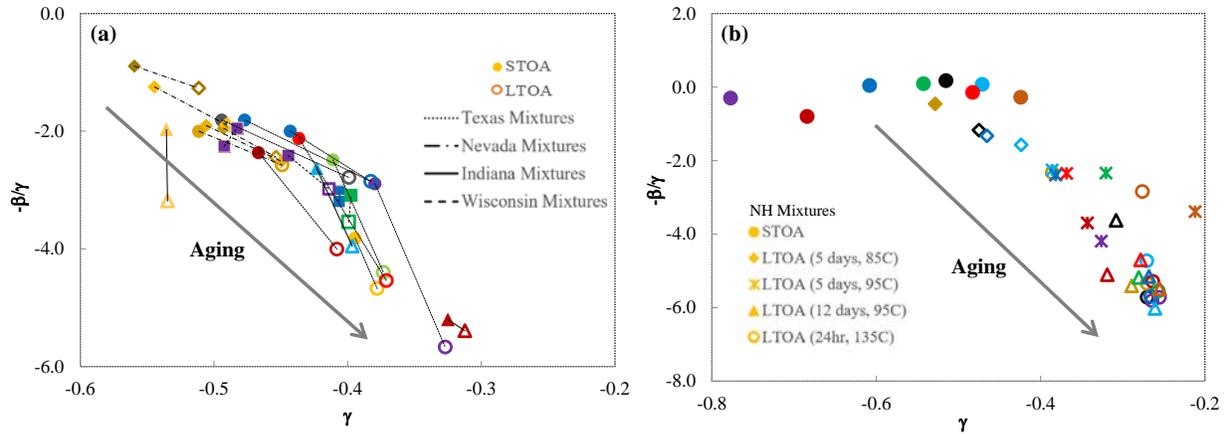
1
2 **FIGURE 2 Shift in Black Space Points (15°C and 5 rad/s) due to Aging (a) NCHRP**
3 **Mixtures (b) New Hampshire Mixtures**
4

5 **- β/γ vs γ parameter** – The regression analysis indicated that the changes in the $-\beta/\gamma$ vs
6 γ parameter are primarily impacted by aging (p-value <0.001). These changes in the $-\beta/\gamma$ vs γ
7 points due to aging are shown in Figures 3 (a) and (b). The plots show that the $-\beta/\gamma$ vs γ
8 points tend to shift towards the bottom right with aging. For NH mixtures the shift increases as the
9 aging level changes from 5 days at 85°C to 5 days at 95°C followed by 12 days at 95°C and 24hr
10 at 135°C which is a similar observation from the Black space plot in Figure 2 (b). This shift
11 occurs due to the movement of the inflection point to the left in the $|E^*|$ master-curve as a result
12 of the change in dominance of the binder at a lower loading frequency due to age induced
13 decrease in viscosity. Moreover, with aging a larger width of the relaxation spectra is exhibited.
14 A combination of the lower relaxation capacity and increased relaxation width results in a
15 mixture that is more susceptible to thermal cracking. The researchers recommend the use of the
16 $-\beta/\gamma$ vs γ plot when tracking changes in mixture properties only due to aging.

17 **- β/γ parameter** - The $-\beta/\gamma$ parameter when considered separately appears to be
18 influenced by both aging and PGLT of the binder. This indicates that a shift in inflection point
19 frequency is mainly a result of a change in these two parameters and can be used to track the
20 changes in material properties due changes in these two mixture variables.

21 **γ parameter** – The statistical analysis shows the ability of the γ parameter to capture the
22 changes due to aging and PGHT of the binder. With aging, the dynamic modulus curve becomes
23 flatter which increases the width of the relaxation spectra resulting in a greater propensity to
24 thermal cracking.

25 **Lower and upper asymptote**- Both lower and upper asymptote appear to be affected by
26 aging whereas only lower asymptote is impacted by PGLT.



1
2 **FIGURE 3 Shift in $-\beta/\gamma$ vs γ Points due to Aging (a) NCHRP Mixtures (b) NH Mixtures**

3
4 It should be noted that all master-curve parameters were able to capture the effect of
5 aging whereas on the contrary the effects of rejuvenator were not captured by any of the
6 parameters. The authors believe that the use of the low dosages and different types of
7 rejuvenators for the mixtures obtained from Texas, Nevada, Indiana and Wisconsin could have
8 impacted the mixture parameters differently resulting in the statistically insignificant effect of the
9 rejuvenator on the rheological properties of the mixture. It is believed that the changes observed
10 in the master-curve parameters can be attributed to changes in mixture field performance.
11 Therefore, these changes can be entered into pavement performance prediction models to
12 quantify the effect of aging level, addition of rejuvenator, recycled material binder content and
13 binder grade on field performance of asphalt concrete mixtures.

14 **4. SUMMARY AND CONCLUSION**

15 In this study master-curve parameters such as the G-R parameter, log of the inflection
16 point frequency ($-\beta/\gamma$), log of the distance between the glassy modulus and the inflection
17 point modulus (γ), $-\beta/\gamma$ vs γ and lower and upper asymptote of the sigmoidal form of master-curve
18 were investigated to identify their ability to distinguish between mixture variables by performing
19 a comprehensive statistical analysis. The evaluated mixture variables included aging level,
20 rejuvenator dosage, RBR, and binder grade. A stepwise regression analysis conducted on the
21 mixtures indicated that the mixture G-R parameter can capture the changes in mixture properties
22 due to aging, RBR, and PGLT whereas the $-\beta/\gamma$ vs γ parameter was able to capture the effect of
23 aging only. A shift of Black space points to the top left has been observed with aging whereas the
24 opposite trend was observed in the $-\beta/\gamma$ vs γ plot which is associated more with cracking
25 susceptibility in both cases.

26 Depending on the mixture specifier's or producer's interest in evaluating the effect of one
27 or more of the mixture variables, the parameters identified in this study can be used to track the
28 changes in rheological properties due to changes in specific mixture variables.

29 It is believed that the changes observed in the master-curve parameters can be attributed
30 to changes in mixture field performance. Therefore, in future work these changes will be used to
31 illustrate the changes in mixture field performance due to the presence of RAP/RAS, addition of
32 rejuvenator, binder grade and aging level. This will be done by quantifying the changes in
33 master-curve parameters and inputting the values into pavement performance prediction models.

1 **5. REFERENCES**

2 [1] American Association of State Highway and Transportation Officials, "Standard
3 Method of Test for Determining Dynamic Modulus of Hot-Mixture Asphalt Concrete Mixtures,"
4 AASHTO T342, 2012.

5 [2] Baumgaertel, M., and H. H. Winter. "Determination of discrete relaxation and
6 retardation time spectra from dynamic mechanical data." *Rheologica Acta* 28, no. 6: 511-519,
7 1989.

8 [3] Park, S. W., and Y. R. Kim. "Interconversion between relaxation modulus and creep
9 compliance for viscoelastic solids." *Journal of materials in Civil Engineering* 11, no. 1 76-82,
10 1999.

11 [4] Bari, Javed, and Matthew Witczak. "Development of a new revised version of the
12 Witczak E* predictive model for hot mixture asphalt mixtures (with discussion)." *Journal of the*
13 *Association of Asphalt Paving Technologists* 75, 2006.

14 [5] Christensen Jr, D. W., T. Pellinen, and R. F. Bonaquist. "Hirsch model for estimating
15 the modulus of asphalt concrete." *Journal of the Association of Asphalt Paving Technologists* 72,
16 2003.

17 [6] Nemati, R. and Dave, E. "Nominal Property Based Predictive Models for Asphalt
18 Mixture Complex Modulus (Dynamic Modulus and Phase Angle)." *Construction and Building*
19 *Materials*, 2017 (In press).

20 [7] Rowe, G. "Phase angle determination and interrelationships within bituminous
21 materials." In *Proceedings of the 7th Int. RILEM Symposium on Advanced Testing and*
22 *Characterization of Bituminous Materials*, Rhodes, Greece, (Book 1, Edited by Loizos, Partl,
23 Scapas & Al-Qadi), May, vol. 27, pp. 43-52, 2009.

24 [8] Oshone, M., Dave, E., Daniel, S. J., and Rowe, M. G., "Prediction of Phase Angles
25 from Dynamic Modulus Data and Implications on Cracking Performance Evaluation," *Journal of*
26 *Association of Asphalt Paving Technologists*, 2017 (In Press).

27 [9] Oshone, M., Elshaer M, Dave E., Daniel J. Evolution of Asphalt Modulus from
28 Falling Weight Deflectometer Tests and Challenges Associated with its Interpretation and
29 Applications: A Case Study using LTPP Data. *The 10th International Conference on the Bearing*
30 *Capacity of Roads, Railways and Airfields*, 2017.

31 [10] Mensching, David J., Geoffrey M. Rowe, and Jo Sias Daniel. "A mixture-based
32 Black Space parameter for low-temperature performance of hot mixture asphalt." *Road Materials*
33 *and Pavement Design* 18, 404-425, 2017.

34 [11] Rowe, G., G. Baumgardner, and M. Sharrock. "Functional forms for master curve
35 analysis of bituminous materials." In *Proceedings of the 7th international RILEM symposium*
36 *ATCBM09 on advanced testing and characterization of bituminous materials*, vol. 1, pp. 81-91,
37 2016.

38 [12] Kaseer, F., F. Yin, E. Arámbula-Mercado, and A. Epps Martin. "Stiffness
39 Characterization of Asphalt Mixtures with High Recycled Materials Contents and Rejuvenators." *Transportation Research Record: Journal of the Transportation Research Board*, No. 2633, pp
40 58-68, 2017.

41 [13] Rowe, G. M. "Interrelationships in rheology for asphalt binder specifications." In
42 *Proceedings of the Fifty-Ninth Annual Conference of the Canadian Technical Asphalt*
43 *Association (CTAA): Winnipeg, Manitoba*, 2014.

44